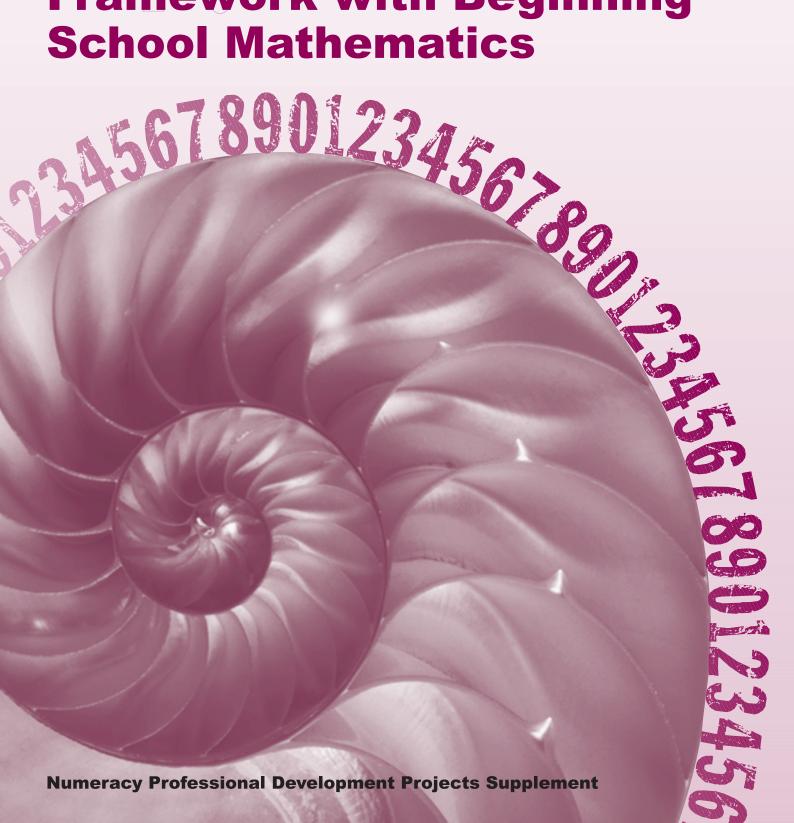
# Enriching the Number Framework with Beginning School Mathematics



#### NUMERACY AND THE CURRICULUM

Numeracy arises out of effective mathematics teaching. All the strands in the mathematics and statistics learning area are important in the pathway to numeracy. Number and Algebra is central to this pathway, although the relative emphasis on this strand changes with the stages of schooling:

- in the first four years of schooling, the main emphasis should be on the Number and Algebra strand;
- in the middle and upper primary years of schooling, the emphasis is spread across the strands of the curriculum;
- towards the end of compulsory schooling, number sense becomes a tool for use across the other strands.

The Venn diagrams in the curriculum statement represent this change in balance across the levels. At all stages, students should:

- create models and predict outcomes, conjecture, justify and verify, and seek patterns and generalisations
- estimate with reasonableness and calculate with precision
- understand when results are precise and when they must be interpreted with uncertainty.

From The New Zealand Curriculum, page 26

Effective numeracy programmes provide students with a range of tools and skills necessary for everyday life and future endeavours.

By studying mathematics and statistics, students develop the ability to think creatively, critically, strategically, and logically. They learn to structure and to organise, to carry out procedures flexibly and accurately, to process and communicate information, and to enjoy intellectual challenge.

The New Zealand Curriculum, page 26

Although the groundwork is laid in mathematics, other curriculum areas also provide opportunities for numeracy learning. In addition, the home, early childhood settings, and the community assist in the development of numeracy.

Numeracy Professional Development Projects Supplement 2008 Published by the Ministry of Education. PO Box 1666, Wellington, New Zealand.

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ISBN 0 478 13216 6 Dewey number 372.7 Topic Dewey number 510 Item number 13216 Note: Teachers may copy these notes for educational purposes.

This book is also available on the New Zealand Maths website, at www.nzmaths.co.nz/Numeracy/2008numPDFs/pdfs.aspx

# Enriching the Number Framework with Beginning School Mathematics Introduction

This booklet is a practical guide to help teachers to effectively use Beginning School Mathematics (BSM) in the delivery of the mathematics and statistics learning area of *The New Zealand Curriculum* in their classrooms. Key BSM activities have been selected to support the teaching and learning of the knowledge and strategies in the Number Framework.

The Numeracy Development Projects and the Beginning School Mathematics resource share these beliefs about mathematics learning:

- Children experience mathematical ideas and develop mathematical skills and understanding before they start school.
- Children learn by relating new ideas to their existing experience and ideas.
- Children learn best when ideas are presented in realistic and meaningful contexts.
- Using equipment is a powerful way of developing children's mathematical understanding.
- Effective mathematics teaching involves a range of approaches.
- Children learn in different ways and at different rates.
- Concepts can be presented in a variety of ways to match different learning styles.
- Learning involves taking risks in a supportive environment.
- The needs of the learner must be at the heart of all planning.
- Feedback can take many forms and is an essential part of the learning process.
- Critical reflection and effective communication of ideas are essential learning tools.

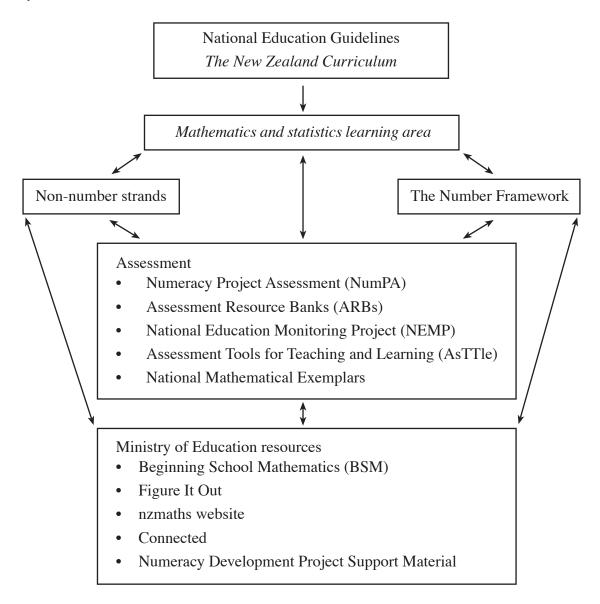
Effective use of BSM by teachers will also support the delivery of the key competencies for the mathematics and statistics learning area of *The New Zealand Curriculum*. Teacher-child interaction will elicit language, develop discussion about strategies, and encourage flexible thinking.

The BSM resource does positively influence children's mathematics learning and their attitudes towards mathematics. The views expressed by teachers, principals, parents and caregivers, together with the reported (and observed) enthusiasm shown by children when they were using the BSM resource, all provide convincing evidence that BSM is a very good resource for the teaching and learning of mathematics in the junior school.

An Evaluation of the Resource Beginning School Mathematics, Ministry of Education, 1996

The possibilities and potential of BSM are as flexible as the teacher, who continues to hold the key to its effective use.

# The Relationships between the Ministry of Education's Mathematics Policy Statements and Resources

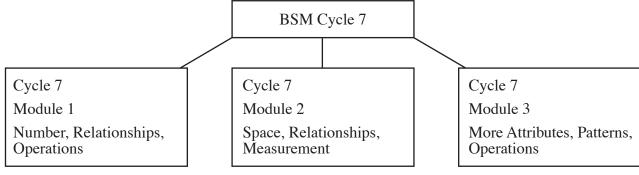


#### Knowing the Beginning School Mathematics Resource

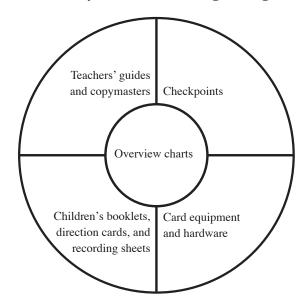
BSM is designed to be used by children in their first three years of schooling. The resource is made up of twelve cycles, and these support all strands of the mathematics and statistics curriculum learning area.

Each cycle is divided into three modules, and each module contains numbered activities. For example, cycle 9, module 3, activity 51 is numbered 9-3-51. The numbering system is consistent throughout the resource and allows the components to be easily identified for borrowing or reshelving.

#### The Structure of Beginning School Mathematics



#### The Components of Beginning School Mathematics



**Overview charts:** There are two overview charts, one covering cycles 1 to 6 and the other cycles 7 to 12. The charts outline the content of each cycle and show how ideas are introduced and developed. The charts reflect the progressions outlined in the knowledge and strategy sections of the Framework.

**Teachers' guides and copymasters:** The teachers' guides contain the aims and objectives, information on mathematical ideas, and suggested developments for learning activities. The copymasters contain material for teachers to use when preparing for teaching. They also contain recording sheets for children.

**Children's booklets, direction cards, and recording sheets:** These components can be used for children to work with independently. They are used with cycles 7 to 12.

**Checkpoints:** There are checkpoints for each cycle. Teachers may find that these contain some useful ideas for checking aspects of children's learning.

**Card equipment and hardware:** Card equipment is supplied to match particular activities in the resource. It is numbered to match the activity (see page 4). Cardware is available from Learning Media Customer Services.

The BSM hardware and other standard mathematical equipment required for BSM activities are described in the teachers' guides. These materials can be obtained from suppliers of educational equipment.

#### Suggested Hardware Materials to Support BSM Activities

Beads and threadersCalculatorsInterlocking cubesClocksMosaic pattern shapesEgg-timers

Cuisenaire® rods Geoboards and rubber bands
Counters Attribute logic blocks
Pegboards and pegs Hundreds boards

Shape/animal/vehicle attribute sets Collections of buttons, bottle tops, shells, stones, acorns, etc.

Pattern boards and blocks Sorting boxes of odds and ends.

Nursery sticks

Refer to *Beginning School Mathematics: A Guide to the Resource*, Learning Media, 1994, for further information about the resource. This book was distributed to schools in 1994. If it is no longer in your school, you can download it from the nzmaths website.

#### Storage

Schools need to ensure that their BSM resource is stored so that teachers can access it easily. It is suggested that schools retain the original organisation of the resource in cycles and modules. Within the classroom, mathematical equipment should also be accessible and easy to retrieve.

#### Linking Beginning School Mathematics to the Number Framework

The tables on pages 6–16 show how BSM activities can be used to support the Number Framework. The tables are arranged according to the five content domains of the knowledge section of the Framework and the three operational domains of the strategy section. The content domains are number identification, number sequence and order, grouping/place value, basic facts, and written recording, and the operational domains are addition/subtraction, multiplication/division, and proportions and ratios.

The BSM activities are identified as being suitable for teacher-led activities (T), class activities (C), and independent activities (I). Many teacher-led learning experiences can become independent activities.

For example:

#### Advanced Counting

#### Stage 4

Knowledge	;					Strategies		
BSM activity	Numeral Identification		Grouping and Place Value	l			Multiplication and Division	
9-1-4	T	T	T					
9-1-42	ΤΙ	I	I					
9-1-6	T		Т	Т	Т			

#### T - Teacher-led activity

C - Class activity

I – Independent activity

The BSM teachers' guides explain how to develop the lesson content to achieve the learning outcomes. Each guide also contains information to reinforce teachers' mathematical content knowledge and pedagogy.

Cycle 1 activities have not been related to the stages of the Number Framework. These learning experiences can be used to help children at the Pre-emergent stage to gain early mathematical understandings. For children at the Emergent stage, the cycle 1 activities will develop language and provide the foundation for further mathematical learning.

Beginning at Stage 2, children need to be taken from the use of materials to imaging (the visualisation of materials). This is not clearly stated in the BSM resource. While no specific activities have been identified for children working at the Counting from One by Imaging stage, teachers can use those activities from the previous stage (Counting from One on Materials) to continue to create strong visual images. They can shield the materials from the children and encourage them to image these materials in order to solve the problem. An empty template has been provided for teachers to record their own selection of activities suitable for use at the Counting from One by Imaging stage.

As number underpins all mathematical learning, the BSM activities relating to other areas (Measurement, Geometry, Algebra, and Statistics) are listed according to the stages of the Number Framework. (See the tables on pages 17–23.) This will enable these to be taught concurrently with number. There is a wealth of learning experiences relating to logic and reasoning in the BSM resource, and these have been listed under each stage. The problem-solving and communication processes are implicit in all activities but will need to be made explicit by the teacher.

With its rich bank of manipulative materials and activities, BSM is an excellent supporting resource for the numeracy projects. Knowledge consolidation is supported through teacher-led activities, many of which can then be used independently. Teachers can select, alter, or adapt activities to meet the changing learning needs of their students.

#### The Use of Questioning

The importance of questioning children about their thinking, giving them time to respond, and giving specific feedback on their responses cannot be overemphasised. Both open and closed questions can be used when working with children.

Teachers are encouraged to share the questions below with:

- parents and caregivers in newsletters and at parents' nights
- children so they can ask each other the questions.

These suggested questions will help to develop children's mathematical thinking and learning:

- Can you tell me how you did that?
- Can you explain what you were thinking as you did that?
- Can you do that another way?
- Could you estimate how many you think it will be?
- How many other ways could you do that?
- How did you do that?
- Is there something you already know that will help you to do this?
- Is that what you thought would happen?
- What did you think of as you worked that out?
- What could we find out?
- What do you want to find out?
- What do you think might happen here?
- What can you tell me about what you have done?
- Tell me how you worked that out.

Teachers can photocopy this page and use it for teaching purposes, school newsletters, and family maths evenings and put it on the wall for children to look at.

#### Schools' Entitlement to BSM Books and Card Equipment

#### **Teachers' Guides**

One copy per teacher of junior classes

#### Students' Books

One copy for every nine students in junior classes

#### **Card Equipment**

One set for every 40 students in junior classes, up to a maximum of four sets

#### Notes:

- Lost or damaged items will be replaced free on request. Only individual items of card equipment will be replaced, not whole sets. We suggest that schools do a stocktake of BSM items each year in October so that orders for replacement can be placed in November with the aim of having a full inventory for the start of term 1 the following year.
- Although teachers' guides are supplied on the basis of one copy per junior class teacher, the books are the property of the school. Teachers moving to another school should expect to find copies available when they arrive.

Schools can obtain these books and equipment from Learning Media Customer Services:

freefax: 0800 800 570

email: orders@learningmedia.co.nz

freephone: 0800 800 565

# BSM Activities Suitable for Each Stage of the Number Framework Emergent Stage 0

Knowledge	2					Strategies		
BSM activity	Numeral Identification	Number Sequence/ Order	Grouping and Place Value	Basic Facts	Written Recording	Addition and Subtraction	Multiplication and Division	Proportions and Ratios
2-1-1			Т			Т	Т	Т
2-1-2			T		I		С	С
2-1-21	T	С	С					
2-1-22			С					
2-1-81			I					
2-1-4	T	С	Т					
2-1-82			I					
2-1-84			ΤΙ					
2-3-7		С						
2-3-24		С						
2-3-8	T	Т	Т					
2-3-13			I					
2-3-55	ΤΙ		ΤΙ					
2-3-81	I		I					
3-1-2	ΤΙ	С						
3-1-21	С	С						
3-1-22	С	С						
3-1-3	ΤΙ	Т	Т					
3-1-49			I					
3-1-4			ΤΙ					
3-1-5	T	Т	T					
3-1-6	T		Т					
3-1-7	T	Т	T					
3-1-23	С	С	С		С			
3-1-45			I					
3-1-46	I	I	I					
3-1-47		I	I					
3-1-81	I		I					
3-1-82	I		I					
3-3-9			Т					
3-3-22		С						
3-3-48	I	I						
3-3-49	I	I						
3-3-81	I	I						

# One-to-one Counting

Stage 1

Knowledge	)					Strategies			
BSM activity	Numeral Identification	Number Sequence/ Order	Grouping and Place Value	Basic Facts	Written Recording	Addition and Subtraction	Multiplication and Division		
2-1-5		Т	Т			Т			
3-1-43		I							
4-1-22	С	С							
4-1-23	С		С			С			
4-1-44	I	I	I						
4-1-45	I	I	I						
4-1-47	I	I							
4-1-48	Т		I						
4-1-83	I	I	I						
4-1-5	Т	Т	Т						
4-1-50	ΤΙ	ΤΙ	TI						
4-1-82	ΤΙ	ΤΙ	TI						
4-3-5		Т	Т						
4-3-6	Т	Т	Т						
4-3-21	С		С			С			
4-3-44	Т		Т			Т			
4-3-84	ΤΙ	ΤΙ	TI						
4-3-46	ΤΙ	I	ΤΙ			Т			
4-3-24	С	С							
4-3-25	С	С							
4-3-51		ΤΙ							
5-1-3	T	Т	Т						
5-1-6	T	Т	Т						
5-1-46	I		I						
5-1-7	T	Т	Т			Т			
5-1-8	Т	С							
5-1-21	С	С							
5-1-22	С	С	С		С				
5-1-83	I	I	I						
5-3-5	Т	Т	Т						
5-3-22		С	С						
5-3-45	I	I	I						
5-3-46	ΤΙ	ΤΙ	TI		ΤΙ				
5-3-82	ΤΙ								
5-3-6		ΤΙ	TI						
5-3-48		I							
5-3-7		ΤΙ	ΤΙ						
5-3-23		С	С						
5-3-49	I		I						
5-3-83			Т						

# One-to-one Counting

# Stage 1 (continued)

Knowledge	)					Strategies	Strategies			
BSM activity	Numeral Identification	Number Sequence/ Order	Grouping and Place Value	Basic Facts	Written Recording	Addition and Subtraction, Place Value	Multiplication and Division	Proportions and Ratios		
6-1-3	T	Т	Т							
6-1-21			С			С				
6-1-4	T	Т	Т							
6-1-43	T		TI			Т				
6-1-5		Т								
6-1-6		Т	Т							
6-1-44	T	I								
6-1-7	T	Т	Т							
6-1-45	I									
6-1-46	T		TI	I		Т				
6-1-81	T		TI	I		Т				
6-1-82			ΤΙ	I		Т				
6-1-9	T		Т			Т				
6-2-21	С									
6-2-22	С									
6-2-9								Т		
6-2-48								Т		
6-3-3	T	Т	Т					I		
7-1-1	T	Т	Т							
7-1-41	I		I							
7-1-42	ΤΙ	TI								
7-1-81	ΤΙ	ΤΙ								
7-1-2					I					
7-1-43					I					
7-1-3		Т								
7-1-44					I					
7-1-46					I					
7-2-7								Т		
7-2-48								ΤΙ		
7-2-49								I		
7-2-82								I		
7-3-4	Т	Т	Т							
8-2-8					ΤΙ			ΤΙ		
8-2-47					ΤΙ			Т		
8-2-48								I		
8-2-83								I		
9-2-18								Т		
9-2-61					TI			ΤΙ		
9-2-85					ΤΙ			ΤΙ		

# Counting from One on Materials Stage 2

Knowledge	;					Strategies			
BSM activity	Numeral Identification	Number Sequence/ Order	Grouping and Place Value	Basic Facts	Written Recording	Addition and Subtraction	Multiplication and Division	Proportions and Ratios	
6-1-3	Т	Т	Т			Т			
6-1-4	Т	Т							
6-1-5		Т							
6-1-6		Т	Т						
6-1-21			С			С			
6-1-7	Т	Т	Т						
6-1-43	Т		ΤΙ			Т			
6-1-44	Т	I							
6-1-45	I								
6-1-46	Т		TI	I		Т			
6-1-81	Т		TI	I		Т			
6-1-82			TI	I		Т			
6-1-9			Т			Т			
6-1-47			T			T			
6-2-9								Т	
6-2-48								Т	
6-3-21	С								
6-3-22	С								
6-3-3	ΤΙ	TI							
6-3-81		Т							
6-3-82						TI			
6-3-4	ΤΙ	TI							
6-3-5	TI		ΤΙ			Т			
6-3-6			I						
6-3-7			Т		Т	T			
6-3-8			ΤΙ		Т	TI			
6-3-49	Т		Т			T			
7-1-1	ΤΙ	TI							
7-1-41	I		I						
7-1-42	ΤΙ	TI							
7-1-81	ΤΙ	ΤΙ							
7-1-2	I				I				
7-1-43	I				I				
7-1-46		ΤΙ							
7-1-82		I							
7-1-48		I							
7-1-49						ΤΙ			
7-1-50						TI			
7-1-6					Т	Т			
7-1-52					I	TI			

# Counting from One on Materials Stage 2 (continued)

Knowledge	)					Strategies		
BSM activity	Numeral Identification	Number Sequence/ Order	Grouping and Place Value	Basic Facts	Written Recording	Addition and Subtraction	Multiplication and Division	Proportions and Ratios
7-1-53					I	ΤΙ		
7-1-85					ΤΙ	ΤΙ		
7-3-4	T	T	T			Т		
7-3-7					Т	Т	Т	
7-3-82					ΤΙ	ΤΙ		
8-1-4	T	T						
8-1-45			Т					
8-1-5			Т		ΤΙ	Т		
8-1-46					I	Т		
8-1-47					I			
8-1-82					I			
8-1-49		T				Т		
8-1-8			T		ΤΙ		Т	
8-1-50					I		TI	
8-1-51					ΤΙ	Т		
8-1-52					ΤΙ	Т		
8-1-83					I	Т		
8-1-84					I			
8-1-10						Т		
8-1-53						ΤΙ		
8-1-85					ΤΙ	Т		
8-3-6								ΤΙ
8-3-47								TI
8-3-48								I
8-3-49								I
8-3-82					I			I
8-3-50					I	Т		
8-3-51					I	Т		
8-3-9					TI	Т		

#### Counting from One by Imaging Stage 3

Knowledge		Strategies		ation Proportions and Ratios				
BSM activity	Numeral Identification	Number Sequence/ Order	Grouping and Place Value	Basic Facts	Written Recording	Addition and Subtraction	Multiplication and Division	Proportions and Ratios

This empty template has been provided for teachers to record their own selection of activities suitable for use at the Counting from One by Imaging Stage. (See page 4.)

# Stage 4

Knowledge	<u> </u>					Strategies			
BSM activity	Numeral Identification	Number Sequence/ Order	Grouping and Place Value	Basic Facts	Written Recording	Addition and Subtraction	Multiplication and Division		
9-1-4	T	Т	Т						
9-1-42	ΤΙ	I	I						
9-1-6	T		Т	Т	Т				
9-1-8					Т	Т			
9-1-45			Т		ΤΙ		Т		
9-1-46			Т		ΤΙ		Т		
9-1-83			ΤΙ		I		Т		
9-1-84			Т		I		Т		
9-1-9			Т		Т				
9-1-10			Т		Т				
9-1-47			Т		I		ΤΙ		
9-1-48			Т				Т		
9-1-12				Т	TI	Т			
9-1-13				Т	TI	Т			
9-1-51				ΤΙ	ΤΙ	Т			
9-1-52				I		I			
9-1-53				I		I			
9-1-54				Т		Т			
9-1-85				I		I			
9-1-86				I		I			
9-1-14					I	Т			
9-1-15					Т	Т			
9-1-16					Т	TI			
9-2-18								ΤΙ	
9-2-61								I	
9-2-85								I	
9-3-48	T		Т			TI			
9-3-84	T				I	Т			
9-3-9		TI							
9-3-51		I							
9-3-52		I							
9-3-10							ΤΙ	Т	
9-3-53							ΤΙ	ΤΙ	
9-3-11					TI	Т			
9-3-12						Т			
9-3-13					ΤΙ	Т			
9-3-55					Т	ΤΙ			
9-3-14					Т	Т			
9-3-58					I	Т			
9-3-85					I	Т			

# Stage 4 (continued)

Knowledge		T				Strategies	T	1
BSM activity	Numeral Identification	Number Sequence/ Order	Grouping and Place Value	Basic Facts	Written Recording	Addition and Subtraction	Multiplication and Division	
10-1-2						Т		
10-1-41					I	Т		
10-1-3	Т	Т	Т		TI			
10-1-42			Т		I	Т		
10-1-82			Т		I	Т		
10-1-4		С	С				С	
10-1-6			Т	Т		Т		
10-1-47			Т	I		Т		
10-1-48			Т	I		Т		
10-1-7				Т		Т		
10-1-49						Т		
10-3-84			Т		I	Т		
10-3-6	Т	Т	Т	Т	Т	Т		
10-3-46					I	Т		
10-3-8				ΤΙ	Т	Т		
10-3-53				I	I	Т		
10-3-9			I	I		Т		
10-3-56			I	I		Т		
10-3-86					I	Т		
10-3-11				Т	Т	Т		
11-1-3						Т		
11-1-6	Т		Т		I	Т	Т	
11-1-47	Т				I	Т		
11-1-48	Т				I	Т		
11-1-7						Т		
11-1-49					I	Т		
11-1-50					I	Т		
11-1-52					I			
11-1-83	Т				I	Т		
11-1-84	Т				I			
11-2-18								Т
11-2-59					Т			Т
11-3-4	Т		Т		I	Т		
11-3-44			I					
11-3-8				Т				
11-3-9	Т					Т		
11-3-50				I	I			
11-3-10						Т		
11-3-12					Т		Т	
11-3-13	Т				Т		Т	

# Stage 4 (continued)

Knowledge	:					Strategies		
BSM activity	Identification		Grouping and Place Value	Basic Facts	Written Recording		Multiplication and Division	. ^ .
11-3-54					I		Т	
11-3-55					I		Т	
12-1-1	Т		Т		ΤΙ			
12-1-5	Т	Т				Т		
12-1-44	Т				I	Т		
12-1-45	Т				I			
12-1-84	Т	Т			I		Т	

# Early Additive Part-Whole

# Stage 5

Knowledge	<del></del>					Strategies		
BSM activity	Numeral Identification	Number Sequence/ Order	Grouping and Place Value	Basic Facts	Written Recording	Addition and Subtraction	Multiplication and Division	
11-3-12			Т			Т	Т	
11-3-13	T		Т		Т	Т		
11-3-54			I			I		
11-3-55			I			I		
12-1-3	T	Т	Т					
12-1-4	T	T	T		Т			
12-1-42	I	I	I					
12-1-43	I	I	I					
12-1-6			T			T		
12-1-46			I			I		
12-1-7				T		Т		
12-1-47				ΤΙ		ΤΙ		
12-1-48	I			I		I		
12-1-49			I			I		
12-1-50	I			I		ΤΙ		
12-1-52				I		I		
12-1-9				T		Т		
12-1-15				I		ΤΙ		
12-1-55					Т	Т		
12-1-56				Т		Т		

# Early Additive Part-Whole

# Stage 5 (continued)

Knowledge	<del></del>		Strategies					
BSM activity	Numeral Identification	Number Sequence/ Order	Grouping and Place Value	Basic Facts	Written Recording	Addition and Subtraction	Multiplication and Division	
12-1-85	Т			I		I		
12-1-86	Т			Т		Т		
12-1-87	Т			I		I		
12-1-89	Т			I		I		
12-3-2	Т			Т	Т	Т		
12-3-45				I	I	I		
12-3-46				I	I	I		
12-3-47				I	I	I		
12-3-81				I		I		
12-3-82	I				I			
12-3-6	С							
12-3-7	Т							T
12-3-49	I							I
12-3-50	I							I
12-3-51	I							I
12-3-83	I							I
12-3-84	I							I
12-3-8	Т			Т		Т		
12-3-52				I	I	I		
12-3-53				I	I	I		
12-3-85	I			I	I	I		
12-3-13				T		Т	Т	

# BSM Activities That Link with other aspects of the mathematics and statistics learning area of *The New Zealand Curriculum*

#### **Emergent**

#### Stage 0

Algebra	Measurement		Geometry		Statistics
Exploring patterns and relationships	Estimating a	nd measuring	Exploring s	hape and space	Statistical investigations
2-3-11	2-1-6	3-1-10	2-2-1	2-2-8	
2-3-12	2-1-7	3-1-24	2-2-2	2-2-9	
2-3-25	2-1-8	3-1-11	2-2-3	2-2-26	
2-3-26	2-1-9	3-2-5	2-2-4	2-2-49	
2-3-27	2-1-24	3-2-6	2-2-21	2-2-85	
3-1-1	2-1-25	3-2-25	2-2-22	2-2-82	
3-1-41	2-1-27	4-1-7	2-2-41	3-2-1	
3-3-10	2-1-43	4-1-8	2-2-43	3-2-2	
3-3-23	2-1-44	4-1-25	2-2-44	3-2-4	
3-3-50	2-1-85	4-1-26	2-2-83	3-2-21	
3-3-51	2-1-86	4-1-51	2-2-23	3-2-22	
	2-1-10	4-1-9	2-2-46	3-2-23	
	2-1-45	4-1-81	2-2-5	3-2-7	
	2-1-12		2-2-6	3-2-24	
	2-1-13		2-2-47		
	2-1-47		2-2-24		
	2-3-23		2-2-25		
Exploring equations and expressions	Developing orate, and cha	concepts of time,	Exploring s transformat	ymmetry and ions	Interpreting statistical reports
	Seriation		-		
	2-1-11		-		
	2-1-11				
	2-3-6				
	2-3-50				
	2-3-50				
	3-1-8				
	3-1-9				
	3-3-7				
T : 1D :	1 2 2 .				1

#### Logic and Reasoning

Interpret information and results in context

2 - 3 - 22, 2 - 3 - 41, 2 - 3 - 42, 2 - 3 - 42, 2 - 3 - 43, 2 - 3 - 44, 2 - 3 - 45, 2 - 3 - 84, 2 - 3 - 85, 2 - 3 - 5, 3 - 3 - 21, 3 - 3 - 41, 3 - 3 - 3, 3 - 3 - 4, 3 - 3 - 44

Classify objects

2-3-1, 2-3-22, 2-3-41, 2-3-2, 2-3-3, 2-3-4, 2-3-21, 2-3-42, 2-3-43, 2-3-44, 2-3-45, 2-3-84, 2-3-85, 2-3-5, 3-3-1, 3-3-42, 3-3-2, 3-3-3, 3-3-43, 3-3-4

#### One-to-one Counting

Stage 1

relationships  4-1-1 4-1-21 4-1-21 4-2-45 4-1-41 4-2-5 4-3-11 4-2-46 4-3-12 4-3-83 4-2-22 4-3-83 5-1-1 5-1-51 5-1-48 5-3-9 5-1-11 5-3-56 5-3-86 5-3-86 5-3-86 5-2-4 5-2-4 5-2-21 5-2-22 5-2-44 5-2-6 5-2-7 5-2-45		3-2-41 3-2-42 3-2-43 3-2-44 3-2-46 3-2-81 3-2-45 3-2-47 4-2-1 4-2-21 4-2-21 4-2-41 4-2-81 4-2-2	5-2-2 5-2-3 5-2-24 5-2-25 5-2-50 5-2-51 5-2-52 6-2-1 6-2-2 6-2-82 6-2-41 6-2-3 6-2-21	Statistical investigations  4-1-1 4-1-26 4-1-41 4-1-2 4-1-21 5-1-2 5-1-84
4-1-21       4-2-45         4-1-41       4-2-5         4-3-11       4-2-46         4-3-83       4-2-22         5-1-1       4-2-23         5-1-51       5-1-48         5-3-9       5-1-11         5-3-11       5-1-49         5-3-86       5-2-5         5-3-6       5-2-43         5-3-48       5-2-81         5-2-21       5-2-22         5-2-44       5-2-6         5-2-7       5-2-45		3-2-42 3-2-43 3-2-44 3-2-46 3-2-81 3-2-45 3-2-47 4-2-1 4-2-21 4-2-21 4-2-81 4-2-2	5-2-3 5-2-24 5-2-25 5-2-50 5-2-51 5-2-52 6-2-1 6-2-2 6-2-82 6-2-41 6-2-3	4-1-26 4-1-41 4-1-2 4-1-21 5-1-2
4-1-41       4-2-5         4-3-11       4-2-46         4-3-12       4-2-82         4-3-83       4-2-22         5-1-1       4-2-23         5-1-51       5-1-48         5-3-9       5-1-11         5-3-56       5-1-50         5-3-86       5-2-5         5-3-6       5-2-43         5-3-48       5-2-81         5-2-4       5-2-21         5-2-22       5-2-44         5-2-6       5-2-7         5-2-45		3-2-43 3-2-44 3-2-46 3-2-81 3-2-45 3-2-47 4-2-1 4-2-21 4-2-41 4-2-81 4-2-2	5-2-24 5-2-25 5-2-50 5-2-51 5-2-52 6-2-1 6-2-2 6-2-82 6-2-41 6-2-3	4-1-41 4-1-2 4-1-21 5-1-2
4-3-11       4-2-46         4-3-12       4-2-82         4-3-83       4-2-22         5-1-1       4-2-23         5-1-51       5-1-48         5-3-9       5-1-11         5-3-11       5-1-49         5-3-86       5-2-5         5-3-6       5-2-43         5-3-48       5-2-81         5-2-21       5-2-22         5-2-44       5-2-6         5-2-7       5-2-45		3-2-44 3-2-46 3-2-81 3-2-45 3-2-47 4-2-1 4-2-21 4-2-41 4-2-81 4-2-2	5-2-25 5-2-50 5-2-51 5-2-52 6-2-1 6-2-2 6-2-82 6-2-41 6-2-3	4-1-2 4-1-21 5-1-2
4-3-12       4-2-82         4-3-83       4-2-22         5-1-1       4-2-23         5-1-51       5-1-48         5-3-9       5-1-11         5-3-11       5-1-49         5-3-56       5-1-50         5-3-86       5-2-5         5-3-6       5-2-43         5-2-41       5-2-81         5-2-21       5-2-21         5-2-24       5-2-6         5-2-45       5-2-45		3-2-46 3-2-81 3-2-45 3-2-47 4-2-1 4-2-21 4-2-41 4-2-81 4-2-2	5-2-50 5-2-51 5-2-52 6-2-1 6-2-2 6-2-82 6-2-41 6-2-3	4-1-21 5-1-2
4-3-83       4-2-22         5-1-1       4-2-23         5-1-51       5-1-48         5-3-9       5-1-11         5-3-11       5-1-49         5-3-86       5-2-5         5-3-6       5-2-43         5-3-48       5-2-81         5-2-4       5-2-21         5-2-22       5-2-44         5-2-6       5-2-7         5-2-45		3-2-81 3-2-45 3-2-47 4-2-1 4-2-21 4-2-41 4-2-81 4-2-2	5-2-51 5-2-52 6-2-1 6-2-2 6-2-82 6-2-41 6-2-3	5-1-2
5-1-1     4-2-23       5-1-51     5-1-48       5-3-9     5-1-11       5-3-11     5-1-49       5-3-56     5-1-50       5-3-86     5-2-5       5-3-6     5-2-43       5-2-41     5-2-21       5-2-22     5-2-44       5-2-6     5-2-7       5-2-45		3-2-45 3-2-47 4-2-1 4-2-21 4-2-41 4-2-81 4-2-2	5-2-52 6-2-1 6-2-2 6-2-82 6-2-41 6-2-3	
5-1-51 5-1-48 5-3-9 5-1-11 5-3-11 5-1-49 5-3-56 5-3-86 5-2-5 5-3-6 5-3-48 5-2-41 5-2-41 5-2-21 5-2-22 5-2-44 5-2-6 5-2-7 5-2-45		3-2-47 4-2-1 4-2-21 4-2-41 4-2-81 4-2-2	6-2-1 6-2-2 6-2-82 6-2-41 6-2-3	5-1-84
5-3-9       5-1-11         5-3-11       5-1-49         5-3-56       5-1-50         5-3-86       5-2-5         5-3-6       5-2-43         5-3-48       5-2-81         5-2-21       5-2-21         5-2-22       5-2-44         5-2-6       5-2-7         5-2-45		4-2-1 4-2-21 4-2-41 4-2-81 4-2-2	6-2-2 6-2-82 6-2-41 6-2-3	
5-3-11 5-1-49 5-3-56 5-1-50 5-3-86 5-2-5 5-3-6 5-2-43 5-3-48 5-2-81 5-2-21 5-2-22 5-2-44 5-2-6 5-2-7 5-2-45		4-2-21 4-2-41 4-2-81 4-2-2	6-2-82 6-2-41 6-2-3	
5-3-56 5-3-86 5-2-5 5-3-6 5-2-43 5-2-4 5-2-21 5-2-22 5-2-44 5-2-6 5-2-7 5-2-45		4-2-41 4-2-81 4-2-2	6-2-41 6-2-3	
5-3-86 5-2-5 5-3-6 5-2-43 5-3-48 5-2-81 5-2-21 5-2-22 5-2-44 5-2-6 5-2-7 5-2-45		4-2-81 4-2-2	6-2-3	
5-3-6 5-2-43 5-3-48 5-2-81 5-2-4 5-2-21 5-2-22 5-2-44 5-2-6 5-2-7 5-2-45		4-2-2		
5-3-48 5-2-81 5-2-4 5-2-21 5-2-22 5-2-44 5-2-6 5-2-7 5-2-45			6 2 21	
5-2-4 5-2-21 5-2-22 5-2-44 5-2-6 5-2-7 5-2-45		1	0-2-21	
5-2-21 5-2-22 5-2-44 5-2-6 5-2-7 5-2-45		4-2-42	6-2-42	
5-2-22 5-2-44 5-2-6 5-2-7 5-2-45		4-2-3	6-2-81	
5-2-44 5-2-6 5-2-7 5-2-45		4-2-43	6-2-83	
5-2-6 5-2-7 5-2-45		4-2-44	7-2-1	
5-2-7 5-2-45		4-2-47	7-2-41	
5-2-45		4-2-25	7-2-42	
		5-2-1	8-2-49	
		5-2-41	8-2-50	
E 1 ' C 1 D 1		5-2-42		
	ping concepts of time, and change	Exploring s	symmetry and tions	Interpreting statistical reports
4-2-6	5-2-23	2-3-9	7-2-2	
4-2-7	5-2-48	2-3-10	7-2-43	
5-2-9	5-2-11	2-3-27	7-2-44	
5-2-10	5-2-49	2-3-53	7-2-81	
Seriati	on	2-3-86	7-2-82	
4-1-7		2-3-87	7-3-5	
5-3-4		3-3-8	7-3-47	
5-3-44		3-3-85	7-3-48	
		5-3-10		
Logic and Reasoning		1		

Interpret information and results in context

 $4 - 3 - 1,\, 4 - 3 - 2,\, 4 - 3 - 3,\, 4 - 3 - 42,\, 4 - 3 - 43,\, 5 - 3 - 1,\, 5 - 3 - 41,\, 5 - 3 - 42,\, 5 - 3 - 2,\, 5 - 3 - 43,\, 5 - 3 - 81,\, 5 - 3 - 3,\, 5 - 3 - 21$ 

Classify objects

4 - 3 - 82, 4 - 3 - 2, 4 - 3 - 3, 4 - 3 - 41, 4 - 3 - 42, 4 - 3 - 43, 4 - 3 - 86, 4 - 3 - 4, 5 - 3 - 1, 5 - 3 - 41, 5 - 3 - 42, 5 - 3 - 2, 5 - 3 - 43, 5 - 3 - 81, 5 - 3 - 3

#### Counting from One on Materials Stage 2

Algebra		Measurer	nent	Geometry	Statistics	
Exploring prelationship	patterns and ps	Estimating	and measuring	Exploring shape and space	Statistical investigations	
6-1-1	7-3-3	6-1-10	8-2-42		6-1-1	
6-1-4	7-3-4	6-2-4	8-2-81		6-1-41	
6-1-6	7-3-6	6-2-43	8-2-2		6-1-2	
6-1-44	7-3-49	6-2-5	8-2-3			
6-3-1	7-3-81	6-2-24	8-2-43			
6-3-3	8-1-1	7-2-3	8-2-4			
6-3-47	8-1-41	7-2-45	8-2-5			
6-3-48	8-1-3	7-2-46	8-2-44			
7-1-42	8-1-43	7-2-4	8-2-45			
7-1-44	8-1-44	7-2-5	8-2-46			
7-1-82	8-1-48	7-2-47				
7-1-4	8-3-5	8-2-1				
7-1-54	8-3-10	8-2-41				
Exploring of expressions	equations and	Developing rate, and ch	concepts of time,	Exploring symmetry and transformations	Interpreting statistical reports	
7-3-3		6-2-7				
7-3-44		6-2-47				
7-3-7		6-2-8				
8-1-3		6-2-23				
8-1-44		7-2-51				
8-3-3		8-2-7				
8-3-44		8-2-46				
8-3-45		8-2-82				
8-3-4		Money		]		
8-3-46		5-2-8				
		6-2-6				
		6-2-22				
		6-2-45				
		6-2-46				
		7-2-6				
		7-2-50				
Logic and	d Reasoning					
Interpret information and results in context						
6-3-1, 6-3-41, 6-3-42, 6-3-51, 7-3-2, 7-3-43						
Classify objects						
6-3-1, 6-3-	41, 6-3-42, 6-3-51,	7-3-1, 7-3-41,	7-3-42, 7-3-2, 7-3-4	43		

#### Counting from One by Imaging Stage 3

Algebra		Measurement	Geometry	Statistics
Exploring patterns and relationships		Estimating and measuring	Exploring shape and space	Statistical investigations
6-1-1	7-3-3			7-1-54
6-1-4	7-3-4			8-1-1
6-1-6	7-3-6			8-1-41
6-1-44	7-3-49			8-1-2
6-3-1	7-3-81			8-1-42
6-3-3	8-1-1			
6-3-47	8-1-41			
6-3-48	8-1-3			
7-1-42	8-1-43			
7-1-44	8-1-44			
7-1-82	8-1-48			
7-1-4	8-3-5			
7-1-54	8-3-10			
Exploring expressions	quations and	Developing concepts of time, rate, and change	Exploring symmetry and transformations	Interpreting statistical reports
7-3-3				
7-3-44				
7-3-7				
8-1-3				
8-1-44				
8-3-3				
8-3-44				
8-3-45				
8-3-4				
8-3-46				
Logic and	Reasoning			
Interpret info	ormation and resul	lts in context		
8-3-2, 8-3-42	2, 8-3-43			
Classify obj	jects			

8-3-1, 8-3-41, 8-3-81 ,8-3-2, 8-3-42, 8-3-43

Stage 4

Algebra		Measurement	Geometry	ý	Statistics
Exploring prelationship		Estimating and measuring	Exploring s	shape and space	Statistical investigations
9-2-48	11-3-82	11-2-12	9-2-1	10-2-6	9-1-1
9-3-82	11-3-14	11-2-48	9-2-41	10-2-7	9-1-2
9-3-5	11-3-15	11-2-49	9-2-42	10-2-8	9-1-3
10-1-6	12-1-1	11-2-50	9-2-43	10-2-45	9-1-41
10-1-47	12-1-2	11-2-51	9-2-44	10-2-46	9-1-81
10-1-48	12-1-41	11-2-83	9-2-81	11-2-1	10-1-1
10-1-83	12-1-81	11-2-13	9-2-6	11-2-2	11-1-1
10-3-11		11-2-14	9-2-7	11-2-41	
10-3-57		11-2-52	9-2-46	11-2-3	
10-3-58		11-2-54	9-2-49	11-2-42	
11-3-4		11-2-53	10-2-1	11-2-43	
11-3-5		12-2-6	10-2-41	11-2-4	
11-3-43		12-2-7	10-2-42	11-2-5	
11-3-44		12-2-48	10-2-81	11-2-44	
11-3-45		12-2-49	10-2-2	11-2-6	
11-3-81		12-2-10	10-2-43	11-2-7	
			10-2-82	11-2-46	
			10-2-83	11-2-8	
			10-2-3	11-2-9	
			10-2-4	11-2-47	
			10-2-5	11-2-82	
			10-2-44		

#### Logic and Reasoning

Interpret information and results in context

11-3-1, 11-3-2, 11-3-41

Classify objects

9-3-1, 9-3-2, 9-3-3, 9-3-41, 9-3-42, 9-3-43, 9-3-81, 9-3-82, 9-3-4, 9-3-44, 10-3-1, 10-3-2, 10-3-3, 10-3-41, 10-3-4, 10-3-5, 10-3-42, 10-3-43, 10-3-44, 10-3-45, 10-3-15, 10-3-61, 10-3-62

# Stage 4 (continued)

Exploring equations and expressions         Developing concepts of time, rate, and change         Exploring symmetry and transformations         Interpreting statistical reports transformations           9-1-11         9-2-16         9-2-82         9-1-1           9-149         9-2-56         9-2-2         9-1-2           9-3-3         9-2-58         9-2-5         9-1-41           9-3-45         9-2-58         9-2-5         9-1-41           9-3-46         10-2-13         9-2-45         9-1-81           9-3-47         10-2-14         10-2-4         10-1-1           10-3-7         10-2-15         10-2-7         11-1-1           10-3-48         10-2-51         10-2-8         11-1-1           10-3-49         10-2-52         10-2-45         10-1-1           10-3-50         11-2-9         10-3-12         10-3-12           10-3-51         11-2-82         10-3-13         10-3-12           11-1-4         11-2-10         10-3-14         11-1-1           11-1-4         11-2-17         10-3-60         11-2-1           11-1-45         11-2-18         11-2-28           11-1-45         11-2-84         11-2-81           11-3-46         92-84         11-2-15	Algebra	Measurement	Geometry	Statistics
9.1-49 9.3-5 9.2-56 9.2-57 9.2-4 9.1-3 9.3-45 9.2-58 9.2-5 9.3-46 10-2-13 9.2-45 9.1-81 9.3-47 10-2-14 10-3-7 10-2-15 10-2-8 10-3-48 10-2-51 10-3-8 10-3-50 11-2-9 10-3-12 10-3-51 11-2-82 10-3-85 11-2-10 11-1-4 11-1-4 11-1-5 11-2-17 11-1-4 11-1-4 11-2-8 11-1-4 11-1-4 11-2-8 11-1-4 11-1-4 11-2-8 11-1-8 11-2-8 11-3-8 11-3-8 11-2-15 11-3-6 11-3-8 11-2-15 11-3-8 11-2-55 11-2-56 12-2-14 12-2-55 Money activities included in Number 12-2-13 12-2-14 12-2-13 12-2-14	Exploring equations and expressions			Interpreting statistical reports
9.3-5 9.2-57 9.2-4 9.1-3 9.3-45 9.2-58 9.2-5 9.1-41 9.3-46 10.2-13 9.2-45 9.1-81 9.3-47 10.2-14 10.2-4 10.1-1 10.3-7 10.2-15 10.2-8 10.3-48 10.2-52 10.2-8 10.3-49 10.2-52 10.2-45 10.3-50 11.2-9 10.3-12 10.3-51 11.2-82 10.3-13 10.3-85 11.2-10 10.3-14 11.1-4 11.2-16 10.3-59 11.1-15 11.2-17 10.3-60 11.1-143 11.2-57 11.2-1 11.1-45 11.2-84 11.2-41 11.1-46 Money 11.3-6 11.3-6 9.2-17 11.3-6 9.2-19 11.3-83 11.2-45 11.2-15 11.2-15 11.2-15 11.2-15 11.2-15 11.2-15 11.2-25 11.2-25 11.2-25 11.2-24 11.3-83 11.2-25 11.2-21 11.3-14 11.2-25 11.2-281 11.3-15 11.2-25 11.2-281 11.3-16 11.2-25 11.2-281 11.3-16 11.2-2-2 11.3-16 11.2-2-2 11.3-16 11.2-2-3-4 11.3-16 11.2-2-3-4 11.3-16 11.2-3-5 11.3-16 11.2-3-5 11.3-16 11.2-3-5 11.3-16 11.2-3-5 11.3-16 11.2-3-5 11.3-16 11.2-3-5 11.3-16 11.2-3-5 11.3-16 11.2-3-5 11.3-16 11.2-3-5 11.3-16 11.2-3-5 11.3-16 11.2-3-5 11.3-16 11.2-3-5 11.3-16 11.3-	9-1-11	9-2-16	9-2-82	9-1-1
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12-2-13 12-2-14 12-2-54				
12-2-14 12-2-54		12-2-43	1	
12-2-54		12-2-13		
12-2-54				
12 2 2 2		12-2-55		

#### Early Additive Part-Whole

#### Stage 5

Algebra	Measurement	Geometry	Statistics
Exploring patterns and relationships	Estimating and measuring	Exploring shape and space	Statistical investigations
12-3-3		12-2-1	
12-3-4		12-2-2	
12-3-81		12-2-42	
12-3-82		12-2-43	
		12-2-3	
		12-2-4	
		12-2-44	
		12-2-45	
		12-2-46	
		12-2-47	
		12-2-16	
Exploring equations and expressions	Developing concepts of time, rate, and change	Exploring symmetry and transformations	Interpreting statistical reports
12-3-3	12-2-8		
12-3-4	12-2-9		
12-3-81	12-2-50		
12-3-82	12-2-51		
	12-2-81		
	Money		
	12-3-12		
	12-3-59		
	12-3-60		
	12-3-89		
	12-3-90		
	12-3-91		
	Money activities included in Number		
	12-3-12	]	
	12-3-59		
	12-3-60		
	12-3-89		
	12-3-90		
	12-3-91		
Logic and Reasoning			
Interpret information and res	ults in context		
12-3-1, 12-3-41, 12-3-42, 12-	-3-43, 12-3-44		

# BSM Activities Recommended for Deletion

Cycle 1			Cycle 6			
			6-1-8	6-2-44	6-3-43	
	Cycle 2	I	6-1-42	6-2-49	6-3-83	
2-1-3	2-2-7	2-3-54	6-1-48			
2-1-26	2-2-42	2-3-83				
2-1-41	2-2-45					
2-1-83	2-2-81					
	2-2-86					
Cycle 3			1			
3-1-42		3-3-46				
3-1-48		3-3-52		Cycle 7		
3-1-50		3-3-53	7-1-47			
3-1-51		3-3-82	7-1-84			
3-1-53		3-3-83				
3-1-54		3-3-84		Cycle 8		
3-1-83					8-3-52	
				Cycle 9		
					9-3-8	
					9-3-49	
					9-3-50	
Cycle 4			Cycle 10			
4-1-52	4-2-83	4-3-7	10-1-5		10-3-10	
4-1-3		4-3-23	10-1-50			
		4-3-47		Cycle 11		
		4-3-49	11-1-8		11-3-11	
		4-3-81	11-1-9			
		4-3-85	11-1-12			
				eference to a learning		
				tions or the Framew		
	Cycle 5		*	still be used but need requires more appro	-	
5-1-9	5-2-46	5-3-24		ng demonstrated.		
5-1-10	5-2-47	5-3-53 (adapt – do it with number dice		s to learning with pla		
5-1-45		instead 1–3)		, 11, and 12 have be		
5-1-51		5-3-54		e children need to be eas with discrete ma		
		5-3-85	example, bundl	les of nursery sticks of	or beans, before	
			being introduced to place value blocks.			
			Items on the deletion list will be deleted from			
			Learning Media stock and will not be reprinted.			

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